# KOHIMA SCIENCE COLLEGE, JOTSOMSA <br> (An Autonomous PG College) <br> DEPARTMENT OF MATHEMATICS 

Subject: Minor changes in the Ph.D. Course Work syllabus.
The total credit point has been changed from 14 points to 16 points by an addition of 2 credit points ( 50 marks) to the paper code MAT-04.

## Revised Syllabus for Course work:

KOHIMA SCIENCE COLLEGE, JOTSOMSA
(An Autonomous PG College)
Ph.D. Course Work Syllabus
MATHEMATICS
Examination Scheme:

| Sl. No | Paper Code | Credit | Name of the Paper | Max. <br> marks |
| :--- | :--- | :---: | :--- | :--- |
| I | MAT-01 | 4 | Research Methodology and <br> Techniques | Quantitative | 100

## I. RESEARCH METHODOLOGY AND QUANTITATIVE TECHNIQUES

Marks: 100

## Unit-1 Research Methodology

Marks: 20
Introduction to Research, importance of research, research methods and research methodology, types of research, selection of research problem, formulation of research problem.

## Unit-2 Manuscript Preparation

Marks: 20
Literature survey, knowledge of web search, importance and typology, Elements of an article:
Title, Abstract, keyword, introduction, formulation, result and discussion, references, research ethics.
Unit-3 Scientific Writing
Marks: 20
Importance of science writing, meaning and nature of scientific style, writing effective scientific prose, effective word selection in science writing, common Mathematical functions and their abbreviation, symbols, operators commonly used in Mathematics.
Unit-4 Typesetting Mathematical Text with LATEX
Marks: 20
Simple document, type style, environments, lists, centering, tables, verbatim, vertical and horizontal spacing, equation environments, fonts, underlying, arrays and matrices, customised commands, document classes and overall structure, title for documents, sectioning commands, inputting files, making a bibliography, making an index.
Unit-5 MATLAB
Marks: 20
Arithmetic operations, built-in functions, scalar variable, creating arrays, Mathematical operations with arrays, script files, programming in MATLAB, solving differential equations. Basic 2-D plots and 3-D Plots.

## Recommended Books:

1. Research Methodology: Methods and Techniques by C. R. Kothari \& G Garg, $4^{\text {th }}$ edn, 2018, New Age international, ISBN: 9789386649225.
2. The Manual of Scientific Style: A Guide for Authors, Editors, and Researchers by Harold Rabinowitz and Suzanne Vogel, 2009, Academic Press, $1^{\text {st }}$ edn, ISBN: 9780123739803.
3. LATEX: A Document Preparation System by Leslie Lamport, 1994, 2nd edn, Pearson, ISBN: 9788177584141.
4. MATLAB Guide by D.J. Higham and N.J. Higham, 2nd edn, 2000, Siam, ISBN: 9780898715163.

## II. GENERAL MATHEMATICS

Marks: 100

## Unit-1: Basic concept of Real and Complex Analysis

Marks: 20
Limits, continuity, uniform continuity, Differentiability, Riemann Integral, Metric space, sequence and series, Algebra of complex numbers, Analytic function, power series, Taylor's and Laurent's Series, conformal mapping.
Unit-2: Basic concept of Linear Algebra
Marks: 20
Vector space, subspace, Linear dependence, linear transformation, algebra of matrices, rank of matrix, determinants, linear equations, Eigen values and Eigen vectors, quadratic forms.
Unit-3: Differential equations
Marks: 20
First order ODE, singular solutions, initial value problem of first order ODE, general theory of homogeneous and non homogeneous linear ODE, variation of parameters.

## Unit 4: Fluid Dynamics

Marks: 20
Lagrangian and Euler methods of description, governing equations of fluid motion, velocity and circulation, equation of continuity equation of energy, motion in two dimension. Viscous fluid, Stokes and Navier equation, steady motion of viscous fluid between two parallel planes, cylindrical pipes.
Unit 5: Differential Geometry
Marks: 20
Space curve, arc length, tangent vectors and vector fields on a curve, curvature and torsion, Serret-Frenet formulae, Osculating plane, osculating circle, osculation sphere, tangent and normal vectors fields on a surface, first, second and third fundamental forms of a surface at a point.

## Recommended Books:

1. A first course in Differential Geometry by Chuan-Chih Hsiung, International Press, 2013, ISBN: 9781571462800.
2. Linear Algebra Done Right by Sheldon Axler, $3^{\text {rd }}$ edn., Springer Nature, ISBN: 9783319110790.
3. Ideal and Incompressible Fluid Dynamics by M.E.O'Neill and F Chorlton, 1986, Prentice Hall, ISBN: 9780134540832.
4. Complex variables and Applications by J.W Brown \& R.V. Churchill, $6^{\text {th }}$ edn., 1996, McGraw Hill, ISBN: 9780071140652.
5. Elementary Differential Equations by W.T. Martin and Eric Relssner, $3^{\text {rd }}$ edn., HoldenDay, 1958, ISBN: 9780816254354.
6. Differential Geometry of Three Dimensions by Weatherburn, 2017, Andesite Press, ISBN: 9781376188677.
III. ADVANCED FLUID DYNAMICS:

Marks: 100
Unit-1: Dimensional Analysis
Marks: 25
Similitude, Geometrical, Kinematic and Dynamical similarity; Dimensionless numbers: Reynolds number, Prandtl number, Eckert number, Grashof number, Nusselt number, Schmidt number, etc; Techniques of dimensional analysis, Rayleigh technique and Buckingham Pi-theorem.

Unit-2: Heat and Mass Transfer
Marks:15+15=30
Heat transfer, the energy equation-conservation of energy, temperature distribution in (i) Couette flow, (ii) Poiseuille flow (iii) Hagen-Poiseuille flow, thermal boundary layer, thermal boundary layer equation in two dimensional flow, free convection and forced convection. Mass transfer, diffusion and convection, Frick's law, concentration boundary layer equation. Unit-3: Finite Difference Method

Marks: 15
Two dimensional parabolic equations- Alternating direction implicit method, the parabolic equation in cylindrical and in spherical polar coordinates, solution of non-linear parabolic equations- A three time level method.

## Unit-4: Finite Volume Method

Marks: 15
Introduction, Differential and integral forms of the general transport equations, the central differencing scheme, properties of discretization schemes, finite volume method for one, two and three dimensional steady state diffusion problem, the power law scheme.

## Unit-5: Perturbation Method

Marks: 15
Perturbation techniques for solving differential equation, homotopy perturbation method.
Recommended Books:

1. Boundary-Layer Theory by H. Schlichting, 2014, $7^{\text {th }}$ edn, McGraw Hill, ISBN: 9789332902824.
2. Heat and Mass Transfer by H.D. Baehr and K. Stephan, 2011, $3^{\text {rd }}$ edn, Springer, ISBN: 9783642200205.
3. Perturbation Methods in Fluid Mechanics by Milton-Von Dyke, 1975, Parabolic Press, ISBN: 9780915760015.
4. Viscous Fluid Dynamics by J.L. Bansal, $2^{\text {nd }}$ edn, Oxford \& IBH, 2003, ISBN: 9788120415942.
5. Convection Heat Transfer by A. Bejan, $4^{\text {th }}$ edn, John Wiley, 2013, ISBN: 9780470900376.
6. Numerical Solutions of Partial Differential Equations: Finite Difference Methods by G.D. Smith, $3^{\text {rd }}$ edn, 1985, Oxford Univ. Press, ISBN: 9780198596509.
7. An Introduction to Computational Fluid Dynamics: The Finite Volume Method by H. K. Versteeg \& W. Malasekera, 2007, PHI, ISBN: 9780131274983.
IV. PROJECT WORK AND SEMINARS

Marks 100

