

October 2025
B.A./B.Sc.
First Semester
MULTI-DISCIPLINARY COURSE – 1
MATHEMATICS
Course Code: MAO 1.11
(Introductory Mathematics)

Total Mark: 50
Time: 2 hours

Pass Mark: 20

I. Answer three questions, taking one from each unit.

UNIT-I

1. (a) Using trigonometric identities show that:
 $\sin 4A = 4 \sin A \cos A - 8 \cos A \sin^3 A$ 3
- (b) Find the principal solution and general solution of $\cos \theta = \frac{\sqrt{3}}{2}$. 4
- (c) A statue, 1.6 m tall, stands on the top of a pedestal. From a point on the ground, the angle of elevation of the top of the statue is 60° and from the same point the angle of elevation of the top of the pedestal is 45° . Find the height of the pedestal. 5
2. (a) Using trigonometric identities, show that:
- (i) $\sin A \sin(60^\circ - A) \sin(60^\circ + A) = \frac{1}{4} \sin 3A$ 3
- (ii) $\frac{\sin x - \sin y}{\cos x + \cos y} = \tan \frac{(x - y)}{2}$ 4
- (b) A TV tower stands vertically on a bank of a canal. From a point A on the other bank directly opposite the tower, the angle of elevation of the top of the tower is 60° . From another point B , 20 m away from A , the angle of elevation of the top of the tower is 30° . Find the height of the tower and the width of the canal from the tower to point A . 4+1=5

UNIT-II

3. (a) Write all the subsets of $A = \{a, b, c\}$. 2
(b) Factorize $(lm+l)+m+1$. 3
(c) Solve the given pair of simultaneous linear equations: 4
 $5x + y = 10$
 $7x - 3y = 14$
(d) Expand the expression $\left(\frac{2}{x} - \frac{x}{2}\right)^5$. 3
4. (a) If $A = \{3, 5, 7, 9, 11\}$, $B = \{7, 9, 11, 13\}$, $C = \{11, 13, 15\}$,
 $D = \{15, 17\}$. Find 4
(i) $A \cup B$
(ii) $A \cap (B \cup D)$
(iii) $A \cap C \cap D$
(iv) $(A \cap B) \cup (C \cap D)$
(b) Find the sum of the first 5 terms of the AP with first term 3 and
common difference 2. 3
(c) Express the partial fraction $\frac{6x^2 + x - 7}{(x-2)^2(x-3)}$. 5

UNIT-III

5. (a) Find the limits of any two of the following: 4
(i) $\lim_{x \rightarrow 1} (x+3)$
(ii) $\lim_{x \rightarrow 3} \left(\frac{x^2 - 9}{x-3}\right)$
(iii) $\lim_{x \rightarrow 2} (x^3 - 1)$
(b) Let $f(x) = \begin{cases} -2, & \text{if } x \leq -1 \\ 2x, & \text{if } -1 < x \leq 1 \\ 2, & \text{if } x \geq 1 \end{cases}$

Discuss the continuity of the function at $x = -1$ and at $x = 1$. 4

(c) Find $\int \frac{1}{(x+1)(x+2)} dx$. 4

6. (a) Find $\frac{dy}{dx}$ when $2x + 3y = \sin x$. 3

(b) Is the function f defined by $f(x) = \begin{cases} x, & \text{if } x \leq 1 \\ 5, & \text{if } x > 1 \end{cases}$ continuous at $x=1$? 4

(c) Find $\int \frac{3x-2}{(x+1)^2(x+3)} dx$. 5

II. Answer any two questions from the following.

7. (a) Find the principal solution and the general solution of $\sin x = \frac{\sqrt{3}}{2}$. 3

(b) From the top a 7 m high building, the angle of elevation of the top of a cable tower is 60° and the angle of depression of its foot is 45° . Determine the height of the cable tower. 4

8. Find the trace, transpose, and the inverse of the matrix

$$A = \begin{bmatrix} 1 & 0 & 2 \\ -1 & 3 & 1 \\ 3 & 4 & 0 \end{bmatrix} \quad 1+1+5=7$$

9. Find the integral of the following:

(a) $\int \frac{x^2 + 1}{x^2 - 5x + 6} dx$ 4

(b) $\int \sin^3 x \cos^2 x dx$ 3