

**2024**  
**M.Sc.**  
**Fourth Semester**  
 CORE – 11  
**PHYSICS**  
*Course Code: MPHC 4.11*  
 (Computational Physics)

*Total Mark: 70*  
*Time: 3 hours*

*Pass Mark: 28*

Answer five questions, taking one from each unit.

**UNIT-I**

1. (a) One of the entry in the following table is incorrect and  $y$  is a cubic polynomial in  $x$ .  
 Use difference table to locate and correct the error. 7
- |     |    |    |    |    |    |    |    |     |
|-----|----|----|----|----|----|----|----|-----|
| $x$ | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7   |
| $y$ | 25 | 21 | 18 | 18 | 27 | 45 | 76 | 123 |
- (b) Find the root of the equation  $x^3 - 2x - 5 = 0$ , using bisection method, correct up to three decimal place. 7
2. (a) Find the root of the equation  $x^4 - x - 10 = 0$ , using Newton-Raphson method correct up to 3 decimal place. 7
- (b) Find the missing term in following table using difference table. 7
- |     |    |      |      |   |      |
|-----|----|------|------|---|------|
| $x$ | 2  | 3    | 4    | 5 | 6    |
| $y$ | 45 | 49.2 | 54.1 | — | 67.4 |

**UNIT-II**

3. (a) Convert the following equations into matrix form
- $$x - 4y - z = -5$$
- $$x + y - 6z = -12$$
- $$3x - y - z = 4$$
- (i) Carry out partial pivoting and  
 (ii) Apply Gauss elimination method to find the value of  $x$ ,  $y$  and  $z$
- 3+5=8

(b) Solve the following equations using Jacobi's method (five iterations).

$$4x + 2z = 4$$

$$5y + 2z = 3$$

$$5x + 4y + 10z = 2 \quad 6$$

4. (a) Find the eigen value and eigen vector of the following matrix. 6

$$A = \begin{bmatrix} 1 & -2 \\ -5 & 4 \end{bmatrix}$$

(b) Using Gauss-Seidel method, solve the following equation

$$20x + y - 2z = 17; 3x + 20y - z = -18; 2x - 3y + 20z = 25 \quad 8$$

### UNIT-III

5. (a) Using Sterling's formula, estimate the value of  $\tan 16^\circ$  8

$$\begin{array}{l} \theta : 0 \quad 5 \quad 10 \quad 15 \quad 20 \quad 25 \quad 30 \\ \tan \theta : 0 \quad 0.0875 \quad 0.1763 \quad 0.2679 \quad 0.3640 \quad 0.4663 \quad 0.5779 \end{array}$$

(b) By the method of least square, find the straight line that best fits the following data: 6

$$\begin{array}{l} x : 1 \quad 2 \quad 3 \quad 4 \quad 5 \\ y : 14 \quad 27 \quad 40 \quad 55 \quad 66 \end{array}$$

6. (a) The table gives the distance ( $x$ ) of the visible horizon for the given height ( $y$ ) above the Earth's surface :

$$\begin{array}{l} x : 100 \quad 150 \quad 200 \quad 250 \quad 300 \quad 350 \quad 400 \\ y : 10.63 \quad 13.03 \quad 15.04 \quad 16.81 \quad 18.42 \quad 19.90 \quad 21.27 \end{array}$$

Using Newton interpolation formula, find the value of  $y$  when  $x$  is 160. 7

(b) Find the polynomial  $f(x)$  by using Lagrange's formula and hence find  $f(3)$  for the following:  $5+2=7$

$$\begin{array}{l} x : 0 \quad 1 \quad 2 \quad 5 \\ f(x) : 2 \quad 3 \quad 12 \quad 147 \end{array}$$

## UNIT-IV

7. (a) Find  $y'(0)$  and  $y''(0)$  from the following table : 7
- |       |   |   |    |   |   |   |
|-------|---|---|----|---|---|---|
| $x :$ | 0 | 1 | 2  | 3 | 4 | 5 |
| $y :$ | 4 | 8 | 15 | 7 | 6 | 2 |
- (b) Evaluate  $\int_0^6 \frac{1}{1+x^2} dx$  by using taking  $h=1$  7
- (i) Trapezoidal rule
- (ii) Simpson's 1/3 rule
8. (a) Using three point Gaussian quadrature formula evaluate  $\int_0^1 \frac{1}{1+x} dx$  . 7
- (b) From the table below, for what value of  $x$ ,  $y$  is minimum? Also find the value of  $y$ . 7
- |       |       |       |       |       |       |       |
|-------|-------|-------|-------|-------|-------|-------|
| $x :$ | 3     | 4     | 5     | 6     | 7     | 8     |
| $y :$ | 0.205 | 0.240 | 0.259 | 0.262 | 0.250 | 0.224 |

## UNIT-V

9. (a) Solve  $\frac{dy}{dx} = 3x + y/2$ ; with  $y(0) = 1$  and  $h = 0.1$ ; find  $y(0.1)$  using R-K 2<sup>nd</sup> order method. 7
- (b) Evaluate  $y(0.1)$  correct up to four decimal places using Taylor's series method, if  $\frac{dy}{dx} = x^2 + y^2$ ;  $y(0) = 1$ . 7
10. Evaluate the function  $u(x, y)$  satisfying the Laplace equation  $\nabla^2 u = 0$  at the pivotal points of the figure shown below: 14

